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**Meta Keywords:** Buck, Power converter, Control loop, External compensation, Current Mode Control (CMC), Frequency response, Bandwidth, Phase margin, Lead, Lag, Crossover frequency

**Meta Description:** How to implement external compensation to optimize the frequency response of the buck switching regulators that use CMC.

**Abstract:** This application note describes how external compensation works and provides a method to implement it with above-mentioned devices. Through external compensation, the frequency response of buck switching regulators is adjusted to increase or decrease the bandwidth of the system by addition of a simple RC network with a feedback circuit.

### **APPLICATION NOTE 7650**

# How to optimize the frequency response of Buck Regulator ICs externally

### Introduction

Most Analog Devices' switching regulators allow the user to adjust the internal control loop. This is typically achieved by varying PGM (programming) components to select alternative configurations from a selection of finite possible configurations. However, if the user requires greater flexibility, then external compensation is implemented. This application note provides the guidelines on the implementation of external compensation for the buck switching regulators that use CMC to optimize its frequency response i.e., increasing or decreasing the bandwidth of the system.

### **Theoretical Overview**

### Why are control loop adjustments needed?

There are several reasons as to why the adjustment of the control loop is needed. Mainly, adjustments are required to resolve an unstable loop. An unstable loop can reduce the performance of a device. This can include the unreasonable oscillation in the output voltage or excessive jittering of the switching waveform.

Alternatively, adjustments to the control loop may be desired by the user to increase the bandwidth of a device, which improves the transient performance. Adjustments may also be required if the user wishes to reduce the output capacitance to reduce BOM but still maintain a stable loop.

**Figure 1** shows the approximate gain magnitude response of a typical buck converter that uses CMC.



Figure 1. Typical buck converter gain magnitude response (CMC).

As shown in **Figure 1**, the typical CMC buck converter frequency response includes an intrinsic pole and zero at  $\omega_0$  and  $\omega_{ESR}$  respectively. The pole  $\omega_0$  is the 'output load pole'. Its location is proportional to the load current applied. And the zero  $\omega_{ESR}$  is generated by the equivalent series resistance (ESR) of output capacitors. Typically, this zero is either canceled by a pole in the device's internal compensation or pushed to a high enough frequency such to make its effects negligible.

Generally, the CMC systems are internally compensated using Type-II compensation (PI) which improves the steady state error and provides flexibility in crossover frequency.

Figure 2 shows the magnitude response of typical CMC with Type-II compensation (Near crossover).



Figure 2. Typical Buck converter gain magnitude response (CMC) with type-II compensation.

Theoretically, after the internal compensation, the magnitude response is simply a straight line with -20dB/dec slope (zoomed in, near the region of crossover).

It is possible that the intrinsic pole and zero, alongside the internal compensation in place, do not give the user's required frequency response. In this case, the user can begin by adjusting the internal control loop of the IC, harnessing the programmability offered by the specific part. An external compensation is needed if this does not meet the user's requirements. This is realized in the form of **lead or lag compensation** by adding RCs (a resistor and capacitor in series) in parallel to the feedback resistors.

### Lead Compensation

The objective of lead compensation is to introduce a zero and a pole at frequencies  $f_Z$  and  $f_P$  respectively, where  $f_Z < f_P$ . The following are the possible motivations to introduce the lead compensation:

- Higher Bandwidth (and therefore reduce rise time and settling time)
- Faster transient response
- Improved Stability (via an increase in Phase Margin)

A possible drawback of lead compensation is that it may increase high-frequency noise. To prevent this, a pole is placed at higher frequency.

**Figure 3** shows the effect that lead compensation has on magnitude and phase. In this example,  $f_{Z}=10$ Hz and  $f_{P}=10$ kHz is used.

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Figure 3. Lead compensation frequency response.

### Lag Compensation

The objective of lag compensation is to introduce a pole and a zero at frequencies  $f_P$  and  $f_Z$  respectively, where  $f_P < f_Z$  (<< BW). The key motivations for using lag compensation are to reduce bandwidth or to improve the steady-state response and have a low DC error.

**Figure 4** shows the effect that lag compensation has on magnitude and phase. In this example,  $f_P=10Hz$  and  $f_Z=10kHz$  is used.



Figure 4. Lag compensation frequency response.

### Control loop Bandwidth (BW) for CMC Buck Converters

For point-of-load buck converters (MAX20710, MAX20812, etc.), the control loop bandwidth is proportional to the feedback divider ratio and calculated by the following equation:

$$BW = \frac{K_{div} * G}{2\pi * C_{out}}$$
(Equation 1)

Where,

 $K_{div} = \frac{R_{fb2}}{R_{fb1} + R_{fb2}}$  is the Feedback Divider from V<sub>out</sub> to V<sub>sense</sub>  $C_{out}$  is the Output Capacitance

*G* is the programmable loop gain (Obtained from the IC data sheet)

For a given "G "and "Cout" (Fixed based on circuit requirements), the BW reduces to:

$$BW = \frac{R_{fb2}}{R_{fb1} + R_{fb2}} * const = K_{div} * const$$
 (Equation 2)

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Therefore, by varying the feedback ratio while maintaining its DC ratio constant (to maintain the required reference voltage), the user can increase or decrease the Bandwidth.

\* Cout is calculated including its derating at rated output voltage

\* This method of external compensation is valid for all ICs with BW proportional to feedback ratio (Follows **Equation 2**)

### **Circuit Implementation**

Lead and lag compensation is implemented by adding RC network (a resistor and capacitor in series) in parallel to the feedback resistors, which are external to the switching regulator IC. For lead compensation (as shown in **Figure 5a**), an RC is added in parallel to the top feedback resistor ( $R_{FB1}$ ). While for lag compensation (as shown in **Figure 5b**), an RC is added in parallel to the bottom feedback resistor ( $R_{FB2}$ ).



Figure 5a. Circuit diagram for lead compensation.



Figure 5b. Circuit diagram for lag compensation.

### Effect of Compensation on loop gain-T(s)

For a buck regulator, a typical loop gain T(s) is shown in **Figure 6**.



Figure 6. Block diagram of a closed loop buck regulator.

The loop gain T(s) is written as:

$$T(s) = G_c(s) * G_{vc}(s) * H(s)$$

Where,

$$H(s) = K_{div} = \frac{R_{fb2}}{R_{fb1} + R_{fb2}}$$
 From (Equation 2)

Where,

 $G_{C}(s)$  is internal compensator TF

 $G_{VC}(s)$  is control to output TF of the buck switching regulator

### 1. Lead compensation:

With lead compensation included, the term H(s) gets modified to the following:

$$H(s)_{lead} = \frac{R_{fb2}}{R_{fb1} || (R_{lead} + \frac{1}{sC_{lead}}) + R_{fb2}}$$

$$H(s)_{lead} = \frac{R_{fb2}}{R_{fb1} + R_{fb2}} * \frac{1 + (R_{fb1} + R_{lead})sC_{lead}}{1 + (R_{fb1}||R_{fb2} + R_{lead})sC_{lead}}$$
(Equation 3)  
DC gain (same as before) Zero and pole added

The series combination of  $R_{lead}$  and  $C_{lead}$  adds a zero and pole at  $f_Z$  and  $f_P$  given by:

$$f_{Z} = \frac{1}{2\pi (R_{fb1} + R_{lead})C_{lead}} \quad \text{and} \quad f_{P} = \frac{1}{2\pi (R_{fb1} || R_{fb2} + R_{lead})C_{lead}}$$
(Result 1)

And it is observed that fz<fp

Thereby, updated loop gain  $T(s)_{lead}$  is:

$$T(s)_{lead} = T(s) * \frac{1 + (R_{fb1} + R_{lead})sC_{lead}}{1 + (R_{fb1}||R_{fb2} + R_{lead})sC_{lead}}$$
(Equation 4)

Equation 4 is further analyzed in detail in the next section.

### 2. Lag compensation:

Like lead, with lag compensation included, the term H(s) gets modified to:

$$H(s)_{lag} = \frac{R_{fb2}||(R_{lag} + \frac{1}{sC_{lag}})}{R_{fb1} + R_{fb2}||(R_{lag} + \frac{1}{sC_{lag}})} * const$$

$$H(s)_{lag} = \frac{R_{fb2}}{R_{fb1} + R_{fb2}} * \frac{1 + (R_{lag})sC_{lag}}{1 + (R_{fb1})|R_{fb2} + R_{lag})sC_{lag}}$$
(Equation 5)
$$DC \text{ gain (same as before)} \qquad \text{pole and zero added}$$

The series combination of  $R_{lag}$  and  $C_{lag}$  adds a zero and pole at  $f_Z$  and  $f_P$  given by:

$$f_{Z} = \frac{1}{2\pi (R_{lag})C_{lag}}$$
 and  $f_{P} = \frac{1}{2\pi (R_{fb1}||R_{fb2} + R_{lag})C_{lag}}$  (Result 2)

And it is observed that fp<fz

Thereby with lag compensation, the loop gain is:

$$T(s)_{lag} = T(s) * \frac{1 + (R_{lag})sC_{lag}}{1 + (R_{fb1}||R_{fb2} + R_{lag})sC_{lag}}$$
(Equation 6)

Equation 3 and 5 confirms that,  $H(s)=K_{div}$  (i.e., directly proportional to BW as per equation 2), gets modified based on the pole-zero pair's location. The added pole-zero pair provides certain gain/attenuation based on the frequency and the values of  $R_{lead/lag}$  and  $C_{lead/lag}$ . This is used to either increase or decrease the current BW.

Hence, adding a series RC network across the feedback resistors modified the system loop gain, which ultimately modified the effective BW of the converter. To analyze the effect of newly added pole and zero, lead and lag compensation are considered separately. Also, the gain provided by the pole-zero pair is dependent on frequency, hence the frequency domain approach of Bode plot is used to analyze the results obtained.

### Analysis of Loop gain with lead compensation

The main objective of lead compensation is to obtain the maximum improvement in BW for the loop gain T(s). This section provides a design method for component selection ( $R_{lead}$  and  $C_{lead}$ ) with goal of obtaining the maximum BW for a given system.

**Figure 7** shows a typical compensated current mode control system. With lead compensation (externally) included, following is the response(shows typical response near the system crossover shown in **Figure 7a**):



Figure 7. Overlay of frequency response of Lead compensated system on typical CMC system.



Figure 7a. Zoomed in version of Figure 7.

It is observed that the newly added zero and pole at  $f_Z$  and  $f_P$  causes the system with lead compensation to have additional gain starting from  $f_Z$ , this effectively causes the BW to improve as the compensated system crosses the 0dB line at BW<sub>new</sub>.

From the plot shown in **Figure 4**, it is concluded through geometry that:

$$\log (f_P) - \log (f_Z) = \log (BW_{new}) - \log (BW_{old})$$

Which implies,

$$BW_{new} = BW_{old} * (f_P / f_Z)$$
 (Equation 7)

Here,

BW<sub>new</sub> - Represents the new crossover frequency with lead compensation

BW<sub>old</sub> - Represents the crossover frequency with no external compensation

**Equation 7** is an important conclusion as it directly links the BW improvement to the ratio of polezero pair frequency. This equation is used to derive values of  $R_{lead}$  and  $C_{lead}$  which provide the maximum bandwidth improvement.

Also, from **Equation 7**, it is clear that, for maximum BW, the pole-zero frequency ratio should be maximum.

Mathematically (substituting result 1 into LHS of Equation 7), the ratio is simplified as:

$$\frac{f_P}{f_Z} = \frac{\left(R_{fb1} + R_{lead}\right)}{\left(R_{fb1} || R_{fb2} + R_{lead}\right)}$$

(Equation 8)

# Maximize this

From analysis, it is observed that the maximum value of **Equation 8** is obtained when:

$$R_{lead} \ll R_{fb1} || R_{fb2}$$

Since the recommended values of R<sub>fb1</sub>, R<sub>fb2</sub> are in between 1k $\Omega$  to 5k $\Omega$ , the user can choose R<sub>lead</sub> to be any value <5 $\Omega$ .

Therefore, for the given values of feedback resistances, the  $BW_{new}$  is calculated as per the **Equation 7a**:

$$BW_{new} = BW_{old} * \frac{R_{fb1}}{R_{fb1} || R_{fb2}}$$
(Equation 7a)

Equation 7a is a useful tool to calculate the maximum BW<sub>new</sub> that is achieved for a given feedback resistance values (i.e., for a given voltage).

With the BW maximized thru careful selection of  $R_{lead}$ , the value of  $C_{lead}$  decides the location of  $f_Z$  and  $f_P$ . The location of the pole-zero pair also affects the Bandwidth and Phase Margin improvement.

To obtain the best possible case, the pole-zero location are swept from low frequency (as low as 100Hz) to the highest frequency possible (determined by  $BW_{old}$ ) by keeping the  $R_{lead}$  constant and varying the  $C_{lead}$  value.

Here, the highest frequency is the one that provides the least value of  $C_{lead}$ , it is obtained when  $f_z=BW_{old}$ . Choosing a frequency higher than this provides no lead compensation for the system. To avoid this, choose  $C_{lead}$  greater than the following:

$$C_{lead} \ge \frac{1}{2\pi * BW_{old} * R_{fb1}}$$

Thorough simulation and hardware testing on multiple system configurations yielded the following results:

- Placement of the pole-zero pair near the highest frequency (before BW<sub>old</sub>) does not provide the maximum improvement in BW as the magnitude plot (actual plot) crosses over much earlier compared to the asymptotic plot. But this method provides a maximum increment in phase margin for the system.
- Placement of the pole-zero pair at lower frequencies (<1kHz) results in a drastic reduction of PM for the system but also provides the maximum improvement in BW.

Therefore, the optimal location of the pole-zero pair is where the BW is maximum, and the PM reduction is minimum. That is found somewhere in-between the high and low frequencies.

Hence, for the maximum improvement in BW with slight reduction in PM, **Equation 9** is used to calculate the value of  $C_{lead}$ . This result is obtained by placing  $f_P$  at 1/10th of BW<sub>old</sub> as shown below:

$$f_P \cong 0.1 * BW_{old}$$

This implies, Clead is calculated as:

$$C_{lead} \cong \frac{10}{2\pi * BW_{old} * R_{fb1} || R_{fb2}}$$
(Equation 9)

Although **Equation 9** provides the best improvement in BW, this value is adjusted to tune the frequency response.

For example, if the requirement of the system is not just maximum BW but improvement in both BW and PM, then the  $C_{lead}$  is decreased to adjust for the best case required. Decreasing the  $C_{lead}$  reduces the BW improvement but increases the PM of the system.

The following are the ranges of Clead:

1. For improvement in both BW and PM but not max BW:

$$\frac{10}{2\pi * BW_{old} * R_{fb1} || R_{fb2}} > C_{lead} \ge \frac{1}{2\pi * BW_{old} * R_{fb1}}$$

2. For maximum BW (with no improvement in PM):

$$C_{lead} \geq \frac{10}{2\pi * BW_{old} * R_{fb1} || R_{fb2}}$$

For case 2, if the Clead increases, the PM of the system decreases.

### Lead Compensation Hardware testing and results

The above theory is tested using the MAX20710 and MAX20812 EV kits. Multiple  $C_{out}$  values were used to verify the concurrence of the theoretical and practical results. The result of one such is shown here.

For the test, a series R-C network is added in parallel with  $R_{fb1}$  for lead compensation and values of the series element calculated using the equations mentioned above. The components used for the experiment have tolerance of 1% ( $R_{lead}$  and  $C_{lead}$ ).

The test conducted uses the **Equation 9** to calculate  $C_{lead}$ . The main aim for the test is to obtain maximum BW with minimum decrease in PM.

Following are the results for each EV kit:

### MAX20710 EV kit results with Cout=1600µF

Following are the values used for the test, it also includes the  $f_Z$  and  $f_P$  values obtained with the components used.

### Table 1. MAX20710 EV Kit Components Values and Other Calculated Quantities

$R_{FB1}$ and $R_{FB2}$	$1.87k\Omega$ and $3.48k\Omega$
V <sub>OUT</sub>	1V
R <sub>LEAD</sub> (Ω)	0
C <sub>LEAD</sub> (Calculated)	19.5nF
C <sub>LEAD</sub> (Used in Ckt)	18.3nF
f <sub>Z</sub> (kHz)	4.67
f <sub>P</sub> (kHz)	7.21

### Table 2. BW and PM with and without Compensation for C<sub>OUT</sub>=1600µF

	BW (kHz)	РМ (°)
NO LOAD		
Uncompensated	67.436	58.876
Lead compensated	98.408	49.769
FULL LOAD – 10A		
Uncompensated	69.285	58.037
Lead compensated	112.604	50.257

According to Equation 7a, the maximum improvement achievable is 103.673kHz.

From the results of **Table 2**, it is observed that the improvement exactly matches the calculated value of  $BW_{new}$  i.e.,  $BW_{old}$  scaled by the pole to zero frequency ratio.

As mentioned earlier, although this method provides the maximum improvement in BW, there is slight reduction in PM of the system (~  $8^{\circ}$ ), mainly attributed due to the lower phase of the system at higher BW. This is adjusted by slightly reducing the value of C<sub>lead</sub>.

Reducing the  $C_{\text{lead}}$  value may reduce the BW slightly but improves the PM as the lead compensation provides some phase boost.

Hence, the **Equation 9** presents the best result for the maximum BW improvement. This is always a good starting point to perform the lead compensation for a first pass result.

**Note:** The maximum BW improvement defers based on the values of  $R_{fb1}$  and  $R_{fb2}$ , i.e., different improvements for different  $V_{out}$ .

As shown in **Figure 8a** and **Figure 8b**, the following are the bode plots of the loop gain for the **Full load=10A** case (values are shown in **Table 2**).



Figure 8a. Shows uncompensated s/m.



Figure 8b. Shows Lead compensated s/m.

The increment in the BW (frequency domain) is directly translated into improvement in the transient response (time domain) of the system, i.e., with an increased BW the system responds quicker to disturbances.

The response is tested using a pulsed load of 2A to 10A with 8A/µs ramp and the results are shown in **Figure 9a** and **Figure 9b**.



Figure 9a. Shows uncompensated s/m with Cout=1600µF.



Figure 9b. Shows Lead compensated s/m with Cout=1600µF.

# Table 3. Overshoot and undershoot with and without Compensation for $C_{OUT}{=}1600 \mu F$

OVERSHOOT			
Uncompensated Overshoot in V <sub>OUT PEAK</sub> (mV)	28.8		
Lead compensated Overshoot in V <sub>OUT PEAK</sub> (mV)	17.7		
$\Delta V_{OUT PEAK}$ - Overshoot reduction (mV)	11.1		
UNDERSHOOT			
Uncompensated Undershoot in V <sub>OUT PEAK</sub> (mV)	30		
Lead compensated Undershoot in V <sub>OUT PEAK</sub> (mV)	21.9		
$\Delta V_{OUT PEAK}$ - Undershoot reduction (mV)	8.1		

It is observed that the undershoots and overshoots during the transient are reduced after improvement in BW by  $\sim$  8 to 10mV. Hence, this is a great way to meet the specification with a last-minute adjustment.

### MAX20812 EV kit results for Cout=870µF

Similar analysis is performed on the MAX20812 EV kit with the following component values shown in **Table 4**.

### Table 4. MAX20812 EV Kit Components Values and Other Calculated Quantities

$R_{FB1}$ and $R_{FB2}$	$3.01$ k $\Omega$ and $3.01$ k $\Omega$
V <sub>OUT</sub>	1V
R <sub>LEAD</sub> (Ω)	0
C <sub>LEAD</sub> (Calculated)	25.6nF
C <sub>LEAD</sub> (Used in Ckt)	25.3nF
f <sub>Z</sub> (kHz)	2.09
f <sub>P</sub> (kHz)	4.18

### Table 5. BW and PM with and without Compensation for C<sub>OUT</sub>=870µF

	BW (kHz)	РМ (°)
NO LOAD		
Uncompensated	41.341	64.924
Lead compensated	78.106	61.112
FULL LOAD - 6A		1
Uncompensated	46.893	68.28
Lead compensated	82.685	62.05

Again, from the **Equation 7a**, the maximum improvement achievable is 82.682kHz.

From results of **Table 5**, it is observed that the improvement exactly matches the calculated value of BW<sub>new</sub>, i.e., BW<sub>old</sub> scaled by the pole to zero frequency ratio.

The reason for more improvement with request to the MAX20710 is due to the difference in  $R_{fb1}$  and  $R_{fb2}$  values in the MAX20812 compared to the MAX20710 for the same output voltage, which ultimately changes the pole to zero frequency ratio in **Equation 7a**. Hence, for a good improvement in BW, the configuration with a lower value of  $R_{fb2}$  (compared to  $R_{fb1}$ ) is preferable.

As shown in **Figure 10a** and **Figure 10b**, the following are the bode plots for the loop gain for a **Full load=6A** (values are shown in **Table 5**).



Figure 10a. Shows uncompensated s/m bode.



Figure 10b. Shows Lead compensated s/m bode.



The transient response improvement for a pulsed load of 1A to 6A with 5A/µs ramp is as follows:

Figure 11a. Shows uncompensated s/m with Cout=870µF.



Figure 11b. Shows Lead compensated s/m with Cout=870µF.

# Table 6. Overshoot and undershoot with and without Compensation for $C_{OUT}{=}870 \mu F$

OVERSHOOT			
Uncompensated Overshoot in V <sub>OUT PEAK</sub> (mV)	48.1		
Lead compensated Overshoot in V <sub>OUT PEAK</sub> (mV)	27.01		
$\Delta$ V_{OUT PEAK} - Overshoot reduction (mV)	21.1		
UNDERSHOOT			
Uncompensated Undershoot in V <sub>OUT PEAK</sub> (mV)	33.5		
Lead compensated Undershoot in V <sub>OUT PEAK</sub> (mV)	22.5		
$\Delta V_{OUT PEAK}$ - Undershoot reduction (mV)	11.1		

The undershoot and overshoot in voltage is reduced by 10mV to 20mV, which is huge, and this is better compared to the previous case of the MAX20710. This is simply due to more increase in BW in the MAX20812 case.

From the above results, it is observed that lead compensation is achieved by the addition of a simple series RC network across  $R_{fb1}$ , where the maximum improvement in BW is limited by the location of  $f_z$  and values of  $R_{fb1}$  and  $R_{fb2}$ . This method of compensation is used to improve the BW only up to a certain extent; therefore, external compensation is used when all other components of the system are fixed with variable  $C_{out}$  requirements. Hence, if there is a

requirement of last-minute BW modification (with/without PM improvement), the lead compensation is the best method to achieve it.

## Loop gain with lag compensation

The main objective of lag compensation is to obtain improvement in phase margin (PM) and reduce the BW of the loop gain T(s) (assuming higher PM at lower BW for the system). This is done in cases where the system has a low  $C_{out}$  value, which causes the BW to near Switching frequency ( $f_{SW}$ ), leading to higher noise in the system.

This section provides a design method for component selection ( $R_{lag}$  and  $C_{lag}$ ) with a goal of reducing the crossover and to obtain improvement in PM at the new BW.

Note: Do not maximize the BW reduction as this decreases the system performance.

**Figure 12** shows a typical compensated current mode control system. With lag compensation included the overlay plot is the response.



Figure 12. Overlay of frequency response of Lag compensated system on typical CMC system.

The design approach is slightly different from the lead compensation method. Here, the PM improvement is obtained from the system (i.e., without external compensation) and not from the lag compensation. In fact, lag compensation has a diminishing effect on the phase of the system as shown in **Figure 4**.

Therefore, for the lag compensated system, the criteria for the best improvement in PM (obtained from the system at a lower BW) is when:

$$BW_{old} \ge 10 * f_Z$$

For calculation, the user can consider the boundary case, i.e.,

$$BW_{old} = 10 * f_Z$$
 or  $f_Z = 0.1 * BW_{old}$ 

Choose  $C_{lag}$ =10nF (to obtain optimum BW reduction and avoid loop instability issues). Increasing the value of  $C_{lag}$  reduces the BW drastically as the f<sub>P</sub> is placed at frequencies less than 500Hz, which causes the gain plot to cross 0dB much faster.

The value of R<sub>lag</sub> is calculated from the **Result 2**, given by:

$$R_{lag} >= \frac{10}{2\pi * C_{lag} * BW_{old}}$$
(Equation 10)

Hence, any value of  $R_{lag}$  greater than or equal to the value from **Equation 10** provides the best result for the lag compensation.

For a lower BW, the  $f_Z$  is shifted further down (i.e.,  $f_Z < 0.1 BW_{old}$ ) by increasing the  $C_{lag}$  and reducing the value of  $R_{lag}$ . This shifts the pole-zero pair to lower frequencies which further improves the PM of the system.

The value of BW<sub>new</sub> obtained with lag compensation from the above R<sub>lag</sub> and C<sub>lag</sub> values provide the minimum reduction in  $f_c$  so that the PM of the compensated system is not reduced due to lag compensation.

### Lag Compensation hardware testing and results

The above theory is tested using both the MAX20710 and MAX20812 EV kits. For the test, a series R-C network is added in parallel with Rfb2, with values for the series element calculated using the equations mentioned above. The components used for the experiment have tolerance of 1% (R<sub>lag</sub> and C<sub>lag</sub>). For both the cases, a C<sub>lag</sub> of 10nF is used (as recommended).

Following are the results for each EV kits:

### MAX20710 EV kit results with Cout=800µF

Following are the values used for the test, it also includes the  $f_Z$  and  $f_P$  values obtained from the components used.

$R_{FB1}$ and $R_{FB2}$	$1.87$ k $\Omega$ and $3.48$ k $\Omega$
V <sub>OUT</sub>	1V
CLAG	10nF
R <sub>LAG</sub> (Calculated)	1.35kΩ
R <sub>LAG</sub> (Used in Ckt)	1.5kΩ
f <sub>Z</sub> (kHz)	12.566
f <sub>P</sub> (kHz)	6.41

### Table 7. MAX20710 EV Kit Components Values and Other Calculated Quantities

	BW (kHz)	РМ (°)	
NO LOAD			
Uncompensated	125.669	37.984	
Lag compensated	84.523	54.438	
FULL LOAD – 6A			
Uncompensated	127.192	38.13	
Lag compensated	83.319	54.198	

### Table 8. BW and PM with and without Compensation for C<sub>OUT</sub>=800µF

From the above results, it is observed that there is an improvement in PM by ~  $20^{\circ}$  with reduction in the crossover frequency or BW. For slight modifications in the crossover, the R<sub>lag</sub> is further adjusted (as explained previously), but this shifts the crossover only by a small margin.

Figure 13a and Figure 13b show the bode response of the loop gain with and without lag compensation at Full load=10A (values are shown in Table 8).



Figure 13a. Shows uncompensated s/m bode.



Figure 13b. Shows Lag compensated s/m bode.

### MAX20812 EV- kit results with C<sub>out</sub>=270.1 $\mu$ F

Similar analysis is performed on the MAX20812 EV kit with the following component values shown in **Table 9**.

### Table 9. MAX20812 EV Kit Components Values and Other Calculated Quantities

$R_{FB1}$ and $R_{FB2}$	$3.01k\Omega$ and $3.01k\Omega$
V <sub>OUT</sub>	1V
C <sub>LAG</sub>	10nF
R <sub>LAG</sub> (Calculated)	1.4249kΩ
R <sub>LAG</sub> (Used in Ckt)	1.42kΩ
f <sub>Z</sub> (kHz)	11.169
f <sub>P</sub> (kHz)	6.025

Table 9 shows the components values and other calculated quantities.

	BW (kHz)	РМ (°)
NO LOAD		
Uncompensated	111.69	55.714
Lag compensated	65.898	63.079
FULL LOAD - 6A		
Uncompensated	131.651	52.574
Lag compensated	70.925	66.9

### Table 10. BW and PM with and without Compensation for C<sub>OUT</sub>=270.1µF

There is an improvement of ~11° in this case, which is lower than the previous case, as this improvement is from the system itself and not dependent on the compensation.

Figure 14a and Figure 14b show the bode plot of both the compensated and uncompensated system, at Full load=6A (values are shown in Table 10).



Figure 14a. Shows uncompensated s/m bode.



Figure 14b. Shows Lead compensated s/m bode.

As mentioned, lag compensation is not used regularly, it is mainly used in cases where the system has low C<sub>out</sub> count (i.e., high crossover frequency).

Although, through this method the user can push the BW to a much lower value, it is recommended not to go lower than 1/10 of  $f_{SW}$ , as the system performance decreases mainly with respect to transient behavior.

Thereby, lag compensation is one of the best methods to improve the PM, with the added benefit of lowering the BW of the system.

# Conclusion

The results obtained for the external compensation hold true for the part numbers mentioned at the beginning of the document. It can also be applied to any other ADI's power management ICs which have the similar form of BW equation, i.e., proportional to the feedback ratio.

In such cases, it is advised to have a DNI/DNP pad for RC network across the feedback resistors, this brings in flexibility during the testing phase of the board to obtain the necessary stability margins.

All said, external compensation is one of the methods to boost the performance of the original system.

### References

- SW Lee. (20014).Demystifying Type II and Type III Compensators Using Op-Amp and OTA for DC/DC Converters (Application Report No. SLVA662). Retrieved from Texas Instruments website: <u>https://www.ti.com/lit/an/slva662/slva662.pdf</u>.
- R. W. Erickson and D. Maksimovic, Fundamentals of Power Electronics, 2nd ed. Norwell, MA, USA: Kluwer, 2001.